restart:
with(DifferentialGeometry) :
$>$ with(Tools):
$>\operatorname{DGsetup}([z, y, u[1], u[2]], M$, verbose $)$;
The following coordinates have been protected:

$$
\left[z, y, u_{1}, u_{2}\right]
$$

The following vector fields have been defined and protected:

$$
\left[D \_z, D \_y, D_{-} u_{1}, D_{-} u_{2}\right]
$$

The following differential 1-forms have been defined and protected:

$$
\begin{align*}
& {\left[d z, d y, d u_{1}, d u_{2}\right]} \\
& \text { frame name: } M \tag{1}
\end{align*}
$$

$\left[\mathrm{M}>\operatorname{LieBracket}\left(L^{\#}, T\right) ;\right.$

$$
\begin{equation*}
4 D \_u_{2} \tag{6}
\end{equation*}
$$

M $>$ Fr $:=$ FrameData $\left(\left[S, T, L, L^{\#}\right], N\right)$;

$$
\operatorname{Fr}:=[[E 2, E 3]=-E 1,[E 2, E 4]=-E 1,[E 3, E 4]=-\mathrm{I} E 2]
$$

$\mathrm{M}>\operatorname{DGsetup}\left(F r,[E],\left[\operatorname{sigma}[0], \operatorname{rho}[0], \operatorname{zeta}[0], \zeta^{\#}[0]\right]\right.$, verbose $)$;
The following coordinates have been protected:

$$
\left[z, y, u_{1}, u_{2}\right]
$$

The following vector fields have been defined and protected:

$$
[E 1, E 2, E 3, E 4]
$$

The following differential 1-forms have been defined and protected:

$$
\left[\sigma_{0}, \rho_{0}, \zeta_{0}, \zeta_{0}^{\#}\right]
$$

$$
\begin{equation*}
\text { frame name: } N \tag{8}
\end{equation*}
$$

$\mathrm{N}>$ ExteriorDerivative $(\operatorname{sigma}[0])$;

$$
\begin{equation*}
\rho_{0} \wedge \zeta_{0}+\rho_{0} \wedge \zeta_{0}^{\#} \tag{9}
\end{equation*}
$$

$\mathrm{N}>$ ExteriorDerivative (rho[0]);

$$
\begin{equation*}
\mathrm{I} \zeta_{0} \wedge \zeta_{0}^{\#} \tag{10}
\end{equation*}
$$

N $>$ ExteriorDerivative(zeta[0]);

$$
\begin{equation*}
0 \sigma_{0} \wedge \rho_{0} \tag{11}
\end{equation*}
$$

| $\mathrm{N}>\operatorname{DGinfo("CurrentFrame");~}$

$$
\begin{equation*}
N \tag{12}
\end{equation*}
$$

$$
\begin{align*}
& {[\mathrm{N}>\operatorname{ChangeFrame}(M)}  \tag{13}\\
& {\left[\begin{array}{l}
\mathrm{M}>\operatorname{DualBasis}\left(\left[S, T, L, L^{\#}\right]\right) ; \\
{\left[\begin{array}{l}
\frac{1}{4} \mathrm{I} y^{2} d z-\frac{1}{4} \mathrm{I} z^{2} d y+\left(-\frac{1}{2} z-\frac{1}{2} y\right) d u_{1}+\frac{1}{4} d u_{2},-\frac{1}{2} \mathrm{I} y d z+\frac{1}{2} \mathrm{I} z d y+\frac{1}{2} d u_{1}, d z, \\
d y
\end{array}\right]} \\
{[\mathrm{M}>}
\end{array}\right.}
\end{align*}
$$

