

```

> restart :
> with(DifferentialGeometry) :
> with(Tools) : with(LinearAlgebra) :
> DGsetup([w, x, y, z, z1], [a, h, h1], frame1, verbose);

```

*The following coordinates have been protected:*

$[w, x, y, z, z1, a, h, h1]$

*The following vector fields have been defined and protected:*

$[D_w, D_x, D_y, D_z, D_z1, D_a, D_h, D_h1]$

*The following differential 1-forms have been defined and protected:*

$[dw, dx, dy, dz, dz1, da, dh, dh1]$

*frame name: frame1*

(1)

Une procédure de dérivation:

```

> Der := proc(x) local y; y := op(1, x) : if (type(x, `+`) = true) then add(Der(op(i, x)), i = 1
.. nops(x)) elif
    (type(x, `*`) = true) then expand( $\frac{x}{y} \cdot Der(y) + y \cdot Der\left(\frac{x}{y}\right)$ ) elif
    (type(x, `^`) = true) then op(2, x) · y(op(2, x) - 1) · Der(y) elif
    ((type(x, function) = true) or (type(x, symbol) = true)) then R(x) · W[1]
+ S(x) · W[2] + Tau(x) · W[3] + L(x) · W[4] + L#(x) · W[5]
    else 0 fi end proc:

```

Les fonctions L et L<sup>#</sup>, Tau, S, et R:

```

> L := proc(x) local y; y := op(1, x) : if (type(x, `+`) = true) then add(L(op(i, x)), i = 1
.. nops(x)) elif
    (type(x, `*`) = true) then expand( $L(y) \cdot \frac{x}{y} + y \cdot L\left(\frac{x}{y}\right)$ ) elif
    (type(x, `^`) = true) then op(2, x) · y(op(2, x) - 1) · L(y) elif
    (type(x, function) = true) then 'L'(x) elif
    (type(x, symbol) = true) then 'L'(x) else 0 fi end proc:

```

```

> L# := proc(x) local y; y := op(1, x) : if (type(x, `+`) = true) then add(L#(op(i, x)), i = 1
.. nops(x)) elif
    (type(x, `*`) = true) then expand( $L^{\#}(y) \cdot \frac{x}{y} + y \cdot L^{\#}\left(\frac{x}{y}\right)$ ) elif
    (type(x, `^`) = true) then op(2, x) · y(op(2, x) - 1) · L#(y) elif
    (type(x, function) = true) then 'L#(x)' elif
    (type(x, symbol) = true) then 'L#(x)' else 0 fi end proc:

```

```

> S := proc(x) local y; y := op(1, x) : if (type(x, `+`) = true) then add(S(op(i, x)), i = 1
.. nops(x)) elif
    (type(x, `*`) = true) then expand( $S(y) \cdot \frac{x}{y} + y \cdot S\left(\frac{x}{y}\right)$ ) elif
    (type(x, `^`) = true) then op(2, x) · y(op(2, x) - 1) · S(y) elif
    (type(x, function) = true) then 'S'(x) elif

```

```

      (type(x, symbol) = true) then 'S'(x) else 0 fi end proc:
> R := proc(x) local y; y := op(1, x) : if (type(x, '+' ) = true) then add(R(op(i, x)), i = 1
  .. nops(x)) elif
      (type(x, '*' ) = true) then expand( R(y) *  $\frac{x}{y}$  + y * R( $\frac{x}{y}$ ) ) elif
      (type(x, '^' ) = true) then op(2, x) * y^(op(2, x) - 1) * R(y) elif
      (type(x, function) = true) then 'R'(x) elif
      (type(x, symbol) = true) then 'R'(x) else 0 fi end proc:
> Tau := proc(x) I * (L(L#(x)) - L#(L(x))) end proc:
> B# :=  $\frac{1}{B}$  : A# := -B# * A :

```

On a normalisé: d=a\*D0 et g= a^2\*G0

Le nouveau coframe initial (tilde, désigné par X), s'exprime en fonction du précédent (chech, désigné par U) par la relation X:=p.U.  
où p est la matrice:

```

> p := Matrix( [[1, 0, 0, 0, 0], [0, 1, 0, 0, 0], [G0, 0, 1, 0, 0], [0, D0, 0, 1, 0], [0, D1, 0, 0,
  1]]) :
> pinv := MatrixInverse(p) :
  U := pinv.Vector([X[1], X[2], X[3], X[4], X[5]]) :

```

On a effectué les normalisations suivantes:  
b= a B0 ; c=a^2 C0 ; f=a^3 F0

Le nouveau coframe initial (chech, désigné par U), s'exprime en fonction du précédent (chapeau, désigné par V) par la relation U:=n.V.  
où n est la matrice:

```

frame1 > n := Matrix( [[1, 0, 0, 0, 0], [F0, 1, 0, 0, 0], [0, C0, 1, 0, 0], [0, 0, B0,
  1, 0], [B1 * B * exp3, B1 * B1/2 * A#, B1, 0, 1]]) :
frame1 > ninv := MatrixInverse(n) :
frame1 > V := ninv.Vector([U[1], U[2], U[3], U[4], U[5]]) :
frame1 >

```

Le coframe chapeau, désigné par V, s'exprime en fonction du coframe initial, W, par la relation V:=m.W.

```

frame1 > m := Matrix( [[ [B-1, 0, 0, 0, 0], [0, B-1/2, 0, 0, 0], [0, 0, 1, 0, 0], [0, 0, 0,
  B-1/2, 0], [0, 0, 0, 0, B1/2]]]) :
frame1 > minv := MatrixInverse(m) :
frame1 > W := minv.Vector([V[1], V[2], V[3], V[4], V[5]]) :

```

On donne ensuite la matrice de groupe:

**frame2** >  $Ma := \text{Matrix}([ [a^4, 0, 0, 0, 0], [0, a^3, 0, 0, 0], [0, 0, a^2, 0, 0], [h, 0, 0, a, 0], [0, a, 0], [h1, 0, 0, 0, a] ])$ ;

$$Ma := \begin{bmatrix} a^4 & 0 & 0 & 0 & 0 \\ 0 & a^3 & 0 & 0 & 0 \\ 0 & 0 & a^2 & 0 & 0 \\ h & 0 & 0 & a & 0 \\ h1 & 0 & 0 & 0 & a \end{bmatrix}$$

(2)

**frame1** >  $MaInv := \text{MatrixInverse}(Ma)$  :

**frame1** >  $\text{evalDG}(\text{ExteriorDerivative}(Ma).MaInv)$ ;

$$\begin{bmatrix} \frac{4 da}{a} & -\frac{0 dw h}{a^5} & -\frac{0 dw h1}{a^5} & \frac{0 dw}{a^3} & \frac{0 dw}{a^2} & \frac{0 dw}{a} & \frac{0 dw}{a} \\ \frac{0 dw}{a^4} & -\frac{0 dw h}{a^5} & -\frac{0 dw h1}{a^5} & \frac{3 da}{a} & \frac{0 dw}{a^2} & \frac{0 dw}{a} & \frac{0 dw}{a} \\ \frac{0 dw}{a^4} & -\frac{0 dw h}{a^5} & -\frac{0 dw h1}{a^5} & \frac{0 dw}{a^3} & \frac{2 da}{a} & \frac{0 dw}{a} & \frac{0 dw}{a} \\ \frac{dh}{a^4} & -\frac{da h}{a^5} & -\frac{0 dw h1}{a^5} & \frac{0 dw}{a^3} & \frac{0 dw}{a^2} & \frac{da}{a} & \frac{0 dw}{a} \\ \frac{dh1}{a^4} & -\frac{0 dw h}{a^5} & -\frac{da h1}{a^5} & \frac{0 dw}{a^3} & \frac{0 dw}{a^2} & \frac{0 dw}{a} & \frac{da}{a} \end{bmatrix}$$

(3)

On obtient la liste des formes de Maurer Cartan:

**frame2** >  $t[1] := \frac{da}{a}$  :

**frame1** >  $t[2] := -\frac{h da}{a^5} + \frac{dh}{a^4}$  :

**frame1** >  $t[3] := \frac{dh1}{a^4} - \frac{da h1}{a^5}$  :

**frame1** >

**frame1** >  $FD := \text{FrameData}([t[1], t[2], t[3], dw, dx, dy, dz, dz1], \text{frame2})$  :

**frame1** >  $\text{DGsetup}(FD, [E], [\text{alpha}[1], \text{alpha}[2], \text{alpha}[3], \text{tau}, \text{sigma}, \text{rho}, \text{zeta}, \zeta^\#], \text{verbose})$  :

*The following coordinates have been protected:*

$[w, x, y, z, z1, a, h, h1]$

*The following vector fields have been defined and protected:*

$[E1, E2, E3, E4, E5, E6, E7, E8]$

*The following differential 1-forms have been defined and protected:*

$[\alpha_1, \alpha_2, \alpha_3, \tau, \sigma, \rho, \zeta, \zeta^\#]$

(4)

Le coframe 'relevé' est noté Y. Il est relié au coframe de base U par la relation  $Y := \text{Ma.X}$ .

**frame2** >  $Y := \text{Vector}([\text{tau}, \text{sigma}, \text{rho}, \text{zeta}, \zeta^\#]) :$

**frame2** >  $X := \text{MaInv}.Y :$

Les equations de courbure sur les  $W[i]$  sont connues:

**M** >  $dW[1] := \text{evalDG}(\text{Tr} \cdot (W[1] \&\text{wedge} W[2]) + \text{Qr} \cdot (W[1] \&\text{wedge} W[3]) + K \cdot (W[1] \&\text{wedge} W[5]) + G \cdot (W[1] \&\text{wedge} W[4]) + \text{Nr} \cdot (W[2] \&\text{wedge} W[3]) + B \cdot (W[2] \&\text{wedge} W[5]) + (W[2] \&\text{wedge} W[4])) :$

**M** >  $dW[2] := \text{evalDG}(\text{Sr} \cdot (W[1] \&\text{wedge} W[2]) + \text{Pr} \cdot (W[1] \&\text{wedge} W[3]) + J \cdot (W[1] \&\text{wedge} W[5]) + F \cdot (W[1] \&\text{wedge} W[4]) + \text{Mr} \cdot (W[2] \&\text{wedge} W[3]) + (L(B) + A) \cdot (W[2] \&\text{wedge} W[5]) + B \cdot (W[3] \&\text{wedge} W[5]) + (W[3] \&\text{wedge} W[4])) :$

**M** >  $dW[3] := \text{evalDG}(\text{Rr} \cdot (W[1] \&\text{wedge} W[2]) + \text{OR} \cdot (W[1] \&\text{wedge} W[3]) + H \cdot (W[1] \&\text{wedge} W[5]) + E \cdot (W[1] \&\text{wedge} W[4]) + \text{Lr} \cdot (W[2] \&\text{wedge} W[3]) + L(A) \cdot (W[2] \&\text{wedge} W[5]) + A \cdot (W[3] \&\text{wedge} W[5]) + I \cdot (W[4] \&\text{wedge} W[5])) :$

**frame2** >

**frame2** >

On en a déjà déduit les équations de courbure du coframe initial chapeau (V) à l'étape précédente:

**frame2** >  $dV[1] := \text{evalDG}(B^{-1} \cdot dW[1] + (\text{Der}(B^{-1}) \&\text{wedge} W[1])) :$

**frame2** >  $dV[2] := \text{evalDG}\left(B^{-\frac{1}{2}} \cdot dW[2] + \left(\text{Der}\left(B^{-\frac{1}{2}}\right) \&\text{wedge} W[2]\right)\right) :$

**frame2** >  $dV[3] := dW[3] :$

**frame2** >  $dV[4] := \text{Der}\left(B^{-\frac{1}{2}}\right) \&\text{wedge} W[4] :$

**frame2** >  $dV[5] := \text{Der}\left(B^{\frac{1}{2}}\right) \&\text{wedge} W[5] :$

Les équations de courbures du coframe U s'en déduisent:

**frame2** >  $dU[1] := \text{evalDG}(dV[1]) :$

**frame2** >  $dU[2] := \text{evalDG}(dV[2] + (\text{Der}(F0) \&\text{wedge} V[1]) + F0 \cdot dV[1]) :$

**frame2** >  $dU[3] := \text{evalDG}(dV[3] + (\text{Der}(C0) \&\text{wedge} V[2]) + C0 \cdot dV[2]) :$

**frame2** >  $dU[4] := \text{evalDG}(dV[4] + (\text{Der}(B0) \&\text{wedge} V[3]) + B0 \cdot dV[3]) :$

**frame2** >  $dU[5] := \text{evalDG}\left(dV[5] + (\text{Der}(B1) \&\text{wedge} V[3]) + B1 \cdot dV[3] + \left(\text{Der}\left(B1 \cdot A^\# \cdot B^{\frac{1}{2}}\right) \&\text{wedge} V[2]\right) + B1 \cdot A^\# \cdot B^{\frac{1}{2}} \cdot dV[2] + (\text{Der}(B1 \cdot B \cdot \text{exp3}) \&\text{wedge} V[1]) + B1 \cdot B \cdot \text{exp3} \cdot dV[1]\right) :$

Les équations de courbures du coframe X s'en déduisent:

**frame2** >  $dX[1] := \text{evalDG}(dU[1]) :$

**frame2** >  $dX[2] := \text{evalDG}(dU[2]) :$

**frame2** >  $dX[3] := \text{evalDG}(dU[3] + (\text{Der}(G0) \&\text{wedge} U[1]) + G0 \cdot dU[1]) :$

**frame2** >  $dX[4] := \text{evalDG}(dU[4] + (\text{Der}(D0) \&\text{wedge} U[2]) + D0 \cdot dU[2]) :$

**frame2** >  $dX[5] := \text{evalDG}(dU[5] + (\text{Der}(D1) \&\text{wedge} U[2]) + D1 \cdot dU[2]) :$

On peut maintenant calculer les équations de courbure du coframe 'relevé':

**frame2** >  $\text{Omega} := \text{map}(\text{evalDG}, \text{Ma.Vector}([dX[1], dX[2], dX[3], dX[4], dX[5]])) :$

**frame2** >  $Mat := map(evalDG, (ExteriorDerivative(Ma).MaInv)) :$

**frame2** >  $Mat2 := Mat \&MatrixWedge Y :$

**frame2** >  $SE := map(evalDG, (Mat2 \&MatrixPlus Omega)) :$

**frame2** >  $List := GenerateForms([alpha[1], alpha[2], alpha[3], tau, sigma, rho, zeta, \zeta^\#], 2) :$

**frame2** >  $Torsion := \mathbf{proc}(S, i, j) \mathbf{local} k, X; k := 8 \cdot (i - 1) - \frac{i \cdot (i - 1)}{2} + j - i; X := GetComponents(S, List); \mathbf{expand}(X[k]); \mathbf{end} \mathbf{proc} :$

**frame2** >  $\mathbf{result} := \mathbf{proc}(l) \mathbf{local} k, t, X; X := 0 : t := \mathbf{expand}(GetComponents(l, List)); \mathbf{for} k \mathbf{from} 1 \mathbf{to} 28 \mathbf{do} X := X + t[k] \cdot List[k] \mathbf{od}; X; \mathbf{end} \mathbf{proc} :$

**frame1** >  $\mathbf{result}(SE[1]);$

$$\begin{aligned}
& 4 \alpha_1 \wedge \tau + \left( -\frac{L^\#(B) DI}{a^3 B^{3/2}} + \frac{L^\#(B) B1 A}{a^3 B^2} + \frac{L^\#(B) B1 C0}{a^3 B^{3/2}} - \frac{L(B) D0}{a^3 \sqrt{B}} + \frac{L(B) B0 C0}{a^3 \sqrt{B}} \right. \\
& + \frac{IC0 L^\#(L(B))}{a^3 B} - \frac{IC0 L(L^\#(B))}{a^3 B} + \frac{S(B)}{a^3 \sqrt{B}} + \frac{h}{a^4} - \frac{B0 G0}{a^3} + \frac{F0 D0}{a^3} + \frac{h1}{a^4} \\
& - \frac{B1 G0}{a^3} + \frac{B B1 exp3}{a^3} + \frac{F0 DI}{a^3} + \frac{Nr G0}{a^3 \sqrt{B}} - \frac{\sqrt{B} G D0}{a^3} + \frac{\sqrt{B} G B0 C0}{a^3} \\
& - \frac{K DI}{a^3 \sqrt{B}} + \frac{K B1 A}{a^3 B} + \frac{K B1 C0}{a^3 \sqrt{B}} - \frac{Qr C0}{a^3} + \frac{\sqrt{B} Tr}{a^3} \left. \right) \tau \wedge \sigma + \left( -\frac{L^\#(B) B1}{a^2 B^{3/2}} \right. \\
& - \frac{L(B) B0}{a^2 \sqrt{B}} + \frac{IL(L^\#(B))}{a^2 B} - \frac{IL^\#(L(B))}{a^2 B} + \frac{F0 B0}{a^2} + \frac{F0 B1}{a^2} - \frac{Nr F0}{a^2 \sqrt{B}} \\
& - \frac{\sqrt{B} G B0}{a^2} - \frac{K B1}{a^2 \sqrt{B}} + \frac{Qr}{a^2} \left. \right) \tau \wedge \rho + \left( \frac{L(B)}{a \sqrt{B}} - \frac{F0}{a} + \frac{\sqrt{B} G}{a} \right) \tau \wedge \zeta \\
& + \left( \frac{L^\#(B)}{a B^{3/2}} - \frac{F0}{a} + \frac{K}{a \sqrt{B}} \right) \tau \wedge \zeta^\# + \left( -\frac{B0}{a} - \frac{B1}{a} + \frac{Nr}{a \sqrt{B}} \right) \sigma \wedge \rho + \sigma \wedge \zeta \\
& + \sigma \wedge \zeta^\#
\end{aligned} \tag{5}$$

**frame2** >  $\mathbf{result}(SE[2]);$

$$\begin{aligned}
& 3 \alpha_1 \wedge \sigma + \left( -\frac{\sqrt{B} F0 G D0}{a^4} - \frac{F0 K DI}{a^4 \sqrt{B}} - \frac{1}{2} \frac{L^\#(B) B1 G0}{a^4 B^{3/2}} + \frac{1}{2} \frac{L^\#(B) B1 exp3}{a^4 \sqrt{B}} \right. \\
& - \frac{C0 F0 D0}{a^4} - \frac{B C0 B1 exp3}{a^4} - \frac{C0 F0 DI}{a^4} + \frac{B F B0 C0}{a^4} + \frac{J B1 C0}{a^4} - \frac{F0 B0 G0}{a^4} \\
& - \frac{F0 B1 G0}{a^4} + \frac{B F0 B1 exp3}{a^4} - \frac{F0 Qr C0}{a^4} - \frac{2 G0 B1 A}{a^4 \sqrt{B}} + \frac{A F0 DI}{a^4 \sqrt{B}} \\
& - \frac{L^\#(F0) B1 C0}{a^4 \sqrt{B}} - \frac{\sqrt{B} L(F0) B0 C0}{a^4} - \frac{1}{2} \frac{F0 L^\#(B) DI}{a^4 B^{3/2}} - \frac{1}{2} \frac{F0 L(B) D0}{a^4 \sqrt{B}}
\end{aligned} \tag{6}$$

$$\begin{aligned}
& - \frac{1}{2} \frac{L(B) B0 G0}{a^4 \sqrt{B}} - \frac{L(B) B1 G0}{a^4 \sqrt{B}} + \frac{\sqrt{B} L(B) B1 \exp3}{a^4} + \frac{L(B) F0 D1}{a^4 \sqrt{B}} + \frac{F0 Nr G0}{a^4 \sqrt{B}} \\
& + \frac{J B1 A}{a^4 \sqrt{B}} + \frac{\sqrt{B} A B1 \exp3}{a^4} - \frac{L^\#(F0) B1 A}{a^4 B} - \frac{\frac{1}{2} IL^\#(L(B)) G0}{a^4 B} \\
& + \frac{\frac{1}{2} IL(L^\#(B)) G0}{a^4 B} + \frac{B Sr}{a^4} - \frac{1}{2} \frac{R(B)}{a^4} - \frac{\sqrt{B} S(F0)}{a^4} - \frac{J D1}{a^4} + \frac{\sqrt{B} F0 Tr}{a^4} \\
& + \frac{F0^2 D0}{a^4} + \frac{F0^2 D1}{a^4} + \frac{1}{2} \frac{L^\#(B) h1}{a^5 B^{3/2}} + \frac{S(B) F0}{a^4 \sqrt{B}} + \frac{F0 h}{a^5} + \frac{F0 h1}{a^5} + \frac{1}{2} \frac{L(B) h}{a^5 \sqrt{B}} \\
& + \frac{L(B) h1}{a^5 \sqrt{B}} + \frac{A h1}{a^5 \sqrt{B}} + \frac{IC0 L(L^\#(F0))}{a^4} - \frac{IC0 L^\#(L(F0))}{a^4} - \frac{\sqrt{B} Pr C0}{a^4} \\
& + \frac{L^\#(F0) D1}{a^4 \sqrt{B}} + \frac{\sqrt{B} L(F0) D0}{a^4} - \frac{C0 h}{a^5} - \frac{C0 h1}{a^5} + \frac{G0 D0}{a^4} + \frac{G0 D1}{a^4} + \frac{Mr G0}{a^4} \\
& - \frac{B F D0}{a^4} + \frac{\sqrt{B} F0 G B0 C0}{a^4} + \frac{F0 K B1 C0}{a^4 \sqrt{B}} + \frac{F0 K B1 A}{a^4 B} + \frac{F0 L(B) B0 C0}{a^4 \sqrt{B}} \\
& + \frac{L^\#(B) B1 A F0}{a^4 B^2} + \frac{L^\#(B) B1 C0 F0}{a^4 B^{3/2}} - \frac{IF0 C0 L(L^\#(B))}{a^4 B} + \frac{IF0 C0 L^\#(L(B))}{a^4 B} \Big) \\
\tau \wedge \sigma & + \left( - \frac{IL(L^\#(F0))}{a^3} + \frac{IL^\#(L(F0))}{a^3} + \frac{F0 B1 L(B)}{a^3 \sqrt{B}} + \frac{F0^2 B0}{a^3} + \frac{F0^2 B1}{a^3} \right. \\
& - \frac{F0^2 Nr}{a^3 \sqrt{B}} + \frac{F0 Qr}{a^3} + \frac{\sqrt{B} Pr}{a^3} - \frac{\sqrt{B} F0 G B0}{a^3} - \frac{F0 K B1}{a^3 \sqrt{B}} + \frac{2 B1 A F0}{a^3 \sqrt{B}} \\
& - \frac{1}{2} \frac{F0 L^\#(B) B1}{a^3 B^{3/2}} + \frac{B B1 \exp3}{a^3} - \frac{Mr F0}{a^3} - \frac{B F B0}{a^3} - \frac{J B1}{a^3} - \frac{\frac{1}{2} IF0 L^\#(L(B))}{a^3 B} \\
& + \frac{\frac{1}{2} IF0 L(L^\#(B))}{a^3 B} + \frac{L^\#(F0) B1}{a^3 \sqrt{B}} + \frac{\sqrt{B} L(F0) B0}{a^3} + \frac{h}{a^4} + \frac{h1}{a^4} \\
& \left. - \frac{1}{2} \frac{F0 L(B) B0}{a^3 \sqrt{B}} \right) \tau \wedge \rho + \left( \frac{1}{2} \frac{F0 L(B)}{a^2 \sqrt{B}} - \frac{F0^2}{a^2} + \frac{\sqrt{B} F0 G}{a^2} - \frac{\sqrt{B} L(F0)}{a^2} \right)
\end{aligned}$$

$$\begin{aligned}
& -\frac{G0}{a^2} + \frac{C0 F0}{a^2} + \frac{BF}{a^2} \Big) \tau \wedge \zeta + \left( \frac{1}{2} \frac{L^\#(B) F0}{a^2 B^{3/2}} - \frac{F0^2}{a^2} + \frac{F0 K}{a^2 \sqrt{B}} - \frac{L^\#(F0)}{a^2 \sqrt{B}} \right. \\
& -\frac{G0}{a^2} + \frac{C0 F0}{a^2} - \frac{F0 L(B)}{a^2 \sqrt{B}} - \frac{AF0}{a^2 \sqrt{B}} + \frac{J}{a^2} \Big) \tau \wedge \zeta^\# + \left( -\frac{F0 B0}{a^2} - \frac{F0 B1}{a^2} \right. \\
& + \frac{Nr F0}{a^2 \sqrt{B}} - \frac{1}{2} \frac{L^\#(B) B1}{a^2 B^{3/2}} - \frac{1}{2} \frac{L(B) B0}{a^2 \sqrt{B}} + \frac{1}{2} \frac{1L(L^\#(B))}{a^2 B} - \frac{1}{2} \frac{1L^\#(L(B))}{a^2 B} \\
& + \frac{D0}{a^2} + \frac{D1}{a^2} - \frac{2 B1 A}{a^2 \sqrt{B}} - \frac{B1 L(B)}{a^2 \sqrt{B}} + \frac{Mr}{a^2} \Big) \sigma \wedge \rho + \left( \frac{F0}{a} + \frac{1}{2} \frac{L(B)}{a \sqrt{B}} \right. \\
& - \frac{C0}{a} \Big) \sigma \wedge \zeta + \left( \frac{F0}{a} + \frac{1}{2} \frac{L^\#(B)}{a B^{3/2}} - \frac{C0}{a} + \frac{L(B)}{a \sqrt{B}} + \frac{A}{a \sqrt{B}} \right) \sigma \wedge \zeta^\# + \rho \wedge \zeta \\
& + \rho \wedge \zeta^\#
\end{aligned}$$

**frame2** > result(SE[3]);

$$\begin{aligned}
2 \alpha_1 \wedge \rho + & \left( -\frac{\sqrt{B} G0 G D0}{a^5} - \frac{G0 K D1}{a^5 \sqrt{B}} + \frac{C0 G0 D0}{a^5} + \frac{C0 G0 D1}{a^5} + \frac{C0 Mr G0}{a^5} \right. \\
& -\frac{B C0 F D0}{a^5} - \frac{C0 J D1}{a^5} - \frac{C0^2 F0 D0}{a^5} - \frac{B C0^2 B1 \exp3}{a^5} - \frac{C0^2 F0 D1}{a^5} \\
& + \frac{B F B0 C0^2}{a^5} + \frac{J B1 C0^2}{a^5} - \frac{L(A) B1 G0}{a^5} + \frac{B L(A) B1 \exp3}{a^5} + \frac{L(A) F0 D1}{a^5} \\
& + \frac{H B1 A}{a^5} - \frac{G0 B1 A^2}{a^5 B} + \frac{1}{2} \frac{C0 L(B) h}{a^6 \sqrt{B}} + \frac{C0 L(B) h1}{a^6 \sqrt{B}} + \frac{1}{2} \frac{C0 L^\#(B) h1}{a^6 B^{3/2}} \\
& + \frac{A G0 D1}{a^5 \sqrt{B}} + \frac{B^{3/2} E B0 C0}{a^5} + \frac{\sqrt{B} H B1 C0}{a^5} - \frac{L^\#(G0) B1 A}{a^5 B} - \frac{L^\#(G0) B1 C0}{a^5 \sqrt{B}} \\
& - \frac{\sqrt{B} L(G0) B0 C0}{a^5} - \frac{F0 L^\#(C0) D1}{a^5 \sqrt{B}} - \frac{\sqrt{B} L^\#(C0) B1 \exp3}{a^5} - \frac{\sqrt{B} F0 L(C0) D0}{a^5} \\
& + \frac{L^\#(C0) B1 G0}{a^5 \sqrt{B}} + \frac{\sqrt{B} L(C0) B0 G0}{a^5} - \frac{G0 L^\#(B) D1}{a^5 B^{3/2}} - \frac{G0 L(B) D0}{a^5 \sqrt{B}} + \frac{G0 F0 D0}{a^5} \\
& + \frac{B G0 B1 \exp3}{a^5} + \frac{G0 F0 D1}{a^5} - \frac{G0 Qr C0}{a^5} - \frac{1 B0 G0 D1}{a^5} + \frac{1 D0 B1 G0}{a^5}
\end{aligned} \tag{7}$$

$$\begin{aligned}
& + \frac{IB0 C0 hl}{a^6} - \frac{Ih B1 C0}{a^6} - \frac{L^\#(C0) hl}{a^6 \sqrt{B}} - \frac{\sqrt{B} L(C0) h}{a^6} + \frac{\sqrt{B} Lr G0}{a^5} - \frac{B^{3/2} E D0}{a^5} \\
& - \frac{\sqrt{B} HDI}{a^5} - \frac{\sqrt{B} Pr C0^2}{a^5} + \frac{L^\#(G0) DI}{a^5 \sqrt{B}} + \frac{\sqrt{B} L(G0) D0}{a^5} - \frac{C0^2 hl}{a^6} + \frac{L(A) hl}{a^6} \\
& - \frac{C0^2 h}{a^6} - \frac{1}{2} \frac{C0 R(B)}{a^5} - \frac{B ORC0}{a^5} + \frac{B C0 Sr}{a^5} - \frac{G0^2 B0}{a^5} - \frac{G0^2 B1}{a^5} + \frac{G0 S(B)}{a^5 \sqrt{B}} \\
& + \frac{G0^2 Nr}{a^5 \sqrt{B}} + \frac{\sqrt{B} G0 Tr}{a^5} + \frac{G0 h}{a^6} + \frac{G0 hl}{a^6} + \frac{1}{2} \frac{C0 L(B) B0 G0}{a^5 \sqrt{B}} \\
& + \frac{1}{2} \frac{C0 F0 L(B) D0}{a^5 \sqrt{B}} + \frac{1}{2} \frac{C0 L^\#(B) B1 exp3}{a^5 \sqrt{B}} - \frac{C0 L(B) B1 G0}{a^5 \sqrt{B}} \\
& + \frac{\sqrt{B} C0 L(B) B1 exp3}{a^5} + \frac{C0 L(B) F0 DI}{a^5 \sqrt{B}} + \frac{1}{2} \frac{C0 L^\#(B) B1 G0}{a^5 B^{3/2}} \\
& + \frac{1}{2} \frac{C0 F0 L^\#(B) DI}{a^5 B^{3/2}} - \frac{2 C0 G0 B1 A}{a^5 \sqrt{B}} + \frac{C0 J B1 A}{a^5 \sqrt{B}} + \frac{G0 K B1 A}{a^5 B} \\
& + \frac{G0 L^\#(B) B1 A}{a^5 B^2} + \frac{\sqrt{B} G0 G B0 C0}{a^5} + \frac{G0 K B1 C0}{a^5 \sqrt{B}} - \frac{IB D0 B1 exp3}{a^5} \\
& - \frac{1}{2} \frac{IC0 L(L^\#(B)) G0}{a^5 B} - \frac{Ih B1 A}{a^6 \sqrt{B}} + \frac{1}{2} \frac{IG0 C0 L^\#(L(B))}{a^5 B} + \frac{IB0 C0 F0 DI}{a^5} \\
& - \frac{ID0 B1 C0 F0}{a^5} + \frac{Ih DI}{a^6} - \frac{ID0 hl}{a^6} + \frac{IL^\#(L(C0)) G0}{a^5} - \frac{IL(L^\#(C0)) G0}{a^5} \\
& + \frac{IC0 L(L^\#(G0))}{a^5} - \frac{IC0 L^\#(L(G0))}{a^5} + \frac{IB B0 C0 B1 exp3}{a^5} - \frac{ID0 B1 A F0}{a^5 \sqrt{B}} \\
& + \frac{IB0 G0 B1 A}{a^5 \sqrt{B}} + \frac{B^{3/2} Rr}{a^5} - \frac{\sqrt{B} S(G0)}{a^5} + \frac{BR(C0)}{a^5} \Big) \tau \wedge \sigma + \left( - \frac{L^\#(B) B1 G0}{a^4 B^{3/2}} \right. \\
& \left. - \frac{IL^\#(L(B)) G0}{a^4 B} + \frac{B C0 B1 exp3}{a^4} - \frac{B F B0 C0}{a^4} - \frac{J B1 C0}{a^4} + \frac{F0 B0 G0}{a^4} \right)
\end{aligned}$$



$$\begin{aligned}
& + \frac{F0 B1 G0}{a^4} + \frac{B OR}{a^4} - \frac{1L(L^\#(G0))}{a^4} + \frac{1L^\#(L(G0))}{a^4} - \frac{L(B) B0 G0}{a^4 \sqrt{B}} \\
& + \frac{1L(L^\#(B)) G0}{a^4 B} - \frac{F0 Nr G0}{a^4 \sqrt{B}} + \frac{\sqrt{B} A B1 exp3}{a^4} + \frac{A hl}{a^5 \sqrt{B}} + \frac{\sqrt{B} Pr C0}{a^4} + \frac{C0 h}{a^5} \\
& + \frac{C0 hl}{a^5} + \frac{1}{2} \frac{F0 L(B) B0 C0}{a^4 \sqrt{B}} + \frac{1}{2} \frac{L^\#(B) B1 C0 F0}{a^4 B^{3/2}} + \frac{2 C0 B1 A F0}{a^4 \sqrt{B}} \\
& + \frac{C0 F0 B1 L(B)}{a^4 \sqrt{B}} - \frac{\frac{1}{2} 1F0 C0 L(L^\#(B))}{a^4 B} + \frac{\frac{1}{2} 1F0 C0 L^\#(L(B))}{a^4 B} - \frac{1B B0 B1 exp3}{a^4} \\
& + \frac{G0 Qr}{a^4} + \frac{L^\#(G0) B1}{a^4 \sqrt{B}} - \frac{\sqrt{B} Lr F0}{a^4} - \frac{B^{3/2} E B0}{a^4} - \frac{\sqrt{B} H B1}{a^4} + \frac{\sqrt{B} L(G0) B0}{a^4} \\
& + \frac{1F0 L(L^\#(C0))}{a^4} - \frac{1F0 L^\#(L(C0))}{a^4} - \frac{1B0 hl}{a^5} + \frac{1B1 h}{a^5} - \frac{C0 Mr F0}{a^4} \\
& - \frac{F0 L^\#(C0) B1}{a^4 \sqrt{B}} + \frac{B1 A^2 F0}{a^4 B} + \frac{L(A) F0 B1}{a^4} - \frac{\sqrt{B} G0 G B0}{a^4} - \frac{G0 K B1}{a^4 \sqrt{B}} \\
& - \frac{\sqrt{B} F0 L(C0) B0}{a^4} - \frac{1B0 B1 A F0}{a^4 \sqrt{B}} \Big) \tau \wedge \rho + \left( \frac{G0 L(B)}{a^3 \sqrt{B}} - \frac{G0 F0}{a^3} + \frac{\sqrt{B} G0 G}{a^3} \right. \\
& - \frac{\sqrt{B} L(G0)}{a^3} - \frac{1}{2} \frac{C0 F0 L(B)}{a^3 \sqrt{B}} - \frac{C0 G0}{a^3} + \frac{C0^2 F0}{a^3} + \frac{B C0 F}{a^3} + \frac{\sqrt{B} L(C0) F0}{a^3} \\
& + \frac{1hl}{a^4} - \frac{1B1 G0}{a^3} + \frac{1B B1 exp3}{a^3} + \frac{1B1 A F0}{a^3 \sqrt{B}} + \frac{1B1 C0 F0}{a^3} + \frac{B^{3/2} E}{a^3} \Big) \tau \wedge \zeta \\
& + \left( \frac{G0 L^\#(B)}{a^3 B^{3/2}} - \frac{G0 F0}{a^3} + \frac{G0 K}{a^3 \sqrt{B}} - \frac{L^\#(G0)}{a^3 \sqrt{B}} - \frac{1}{2} \frac{C0 L^\#(B) F0}{a^3 B^{3/2}} - \frac{C0 G0}{a^3} \right. \\
& + \frac{C0^2 F0}{a^3} - \frac{C0 F0 L(B)}{a^3 \sqrt{B}} + \frac{C0 J}{a^3} + \frac{L^\#(C0) F0}{a^3 \sqrt{B}} + \frac{1B0 G0}{a^3} - \frac{1B0 C0 F0}{a^3} - \frac{1h}{a^4} \\
& - \frac{A G0}{a^3 \sqrt{B}} - \frac{L(A) F0}{a^3} + \frac{\sqrt{B} H}{a^3} \Big) \tau \wedge \zeta^\# + \left( -\frac{B0 G0}{a^3} - \frac{B1 G0}{a^3} + \frac{Nr G0}{a^3 \sqrt{B}} \right. \\
& - \frac{1}{2} \frac{L^\#(B) B1 C0}{a^3 B^{3/2}} - \frac{1}{2} \frac{L(B) B0 C0}{a^3 \sqrt{B}} + \frac{\frac{1}{2} 1C0 L(L^\#(B))}{a^3 B} - \frac{\frac{1}{2} 1C0 L^\#(L(B))}{a^3 B}
\end{aligned}$$

$$\begin{aligned}
& + \frac{C0 D0}{a^3} + \frac{C0 D1}{a^3} - \frac{2 C0 B1 A}{a^3 \sqrt{B}} - \frac{C0 B1 L(B)}{a^3 \sqrt{B}} + \frac{C0 Mr}{a^3} + \frac{L^\#(C0) B1}{a^3 \sqrt{B}} \\
& + \frac{\sqrt{B} L(C0) B0}{a^3} - \frac{IB0 D1}{a^3} + \frac{IL^\#(L(C0))}{a^3} - \frac{IL(L^\#(C0))}{a^3} + \frac{IB0 B1 A}{a^3 \sqrt{B}} \\
& + \frac{IB1 D0}{a^3} + \frac{ADI}{a^3 \sqrt{B}} - \frac{B1 A^2}{a^3 B} - \frac{L(A) B1}{a^3} + \frac{\sqrt{B} Lr}{a^3} \left. \right\} \sigma \wedge \rho + \left( \frac{G0}{a^2} \right. \\
& + \frac{1}{2} \frac{C0 L(B)}{a^2 \sqrt{B}} - \frac{C0^2}{a^2} - \frac{\sqrt{B} L(C0)}{a^2} + \frac{ID1}{a^2} - \frac{IB1 A}{a^2 \sqrt{B}} - \frac{IB1 C0}{a^2} \left. \right) \sigma \wedge \zeta + \left( \frac{G0}{a^2} \right. \\
& + \frac{1}{2} \frac{C0 L^\#(B)}{a^2 B^{3/2}} - \frac{C0^2}{a^2} + \frac{C0 L(B)}{a^2 \sqrt{B}} - \frac{L^\#(C0)}{a^2 \sqrt{B}} - \frac{ID0}{a^2} + \frac{IB0 C0}{a^2} + \frac{L(A)}{a^2} \left. \right) \sigma \wedge \zeta^\# \\
& + \left( \frac{C0}{a} + \frac{IB1}{a} \right) \rho \wedge \zeta + \left( \frac{C0}{a} - \frac{IB0}{a} + \frac{A}{a \sqrt{B}} \right) \rho \wedge \zeta^\# + I \zeta \wedge \zeta^\#
\end{aligned}$$

**frame2** > result(SE[4]);

$$\begin{aligned}
& \alpha_1 \wedge \zeta + \alpha_2 \wedge \tau + \left( - \frac{IL(L^\#(D0)) G0}{a^6} + \frac{IL^\#(L(D0)) G0}{a^6} + \frac{h^2}{a^8} + \frac{BR(D0)}{a^6} \right. \\
& - \frac{2 B1 A G0 D0}{\sqrt{B} a^6} + \frac{B0 A G0 D1}{\sqrt{B} a^6} + \frac{\sqrt{B} B0 H B1 C0}{a^6} + \frac{D0 F0 Nr G0}{\sqrt{B} a^6} - \frac{D0 F0 K D1}{\sqrt{B} a^6} \\
& + \frac{D0 A F0 D1}{\sqrt{B} a^6} + \frac{D0 J B1 A}{\sqrt{B} a^6} + \frac{\sqrt{B} D0 A B1 exp3}{a^6} - \frac{B0 A C0 h1}{\sqrt{B} a^7} + \frac{\sqrt{B} h G B0 C0}{a^7} \\
& + \frac{h K B1 C0}{\sqrt{B} a^7} - \frac{1}{2} \frac{D0 L(B) B0 G0}{\sqrt{B} a^6} - \frac{1}{2} \frac{D0 F0 L^\#(B) D1}{B^{3/2} a^6} - \frac{1}{2} \frac{L^\#(B) D1 B0 G0}{B^{3/2} a^6} \\
& + \frac{1}{2} \frac{L^\#(B) h1 B0 C0}{B^{3/2} a^7} - \frac{\sqrt{B} D0 L(F0) B0 C0}{a^6} - \frac{D0 L^\#(F0) B1 C0}{\sqrt{B} a^6} \\
& + \frac{\sqrt{B} C0 L^\#(B0) B1 exp3}{a^6} + \frac{\sqrt{B} L(B0) D0 C0 F0}{a^6} + \frac{L^\#(B0) D1 C0 F0}{\sqrt{B} a^6} \\
& + \frac{1}{2} \frac{h L^\#(B) B1 C0}{B^{3/2} a^7} + \frac{h L(B) B0 C0}{\sqrt{B} a^7} - \frac{L^\#(D0) B1 C0 F0}{\sqrt{B} a^6} - \frac{\sqrt{B} L(D0) B0 C0 F0}{a^6} \\
& + \frac{1}{2} \frac{h L^\#(B) B1 A}{B^2 a^7} - \frac{D0 F0 Qr C0}{a^6} - \frac{D0 F0 B1 G0}{a^6} - \frac{D0 F0 B0 G0}{a^6} + \frac{D0 J B1 C0}{a^6}
\end{aligned} \tag{8}$$

$$\begin{aligned}
& - \frac{B D0 C0 B1 \exp3}{a^6} + \frac{B D0 F B0 C0}{a^6} - \frac{B0 G0 B1 A^2}{B a^6} + \frac{B0 H B1 A}{a^6} + \frac{h K B1 A}{B a^7} \\
& + \frac{B0 L(A) F0 D1}{a^6} + \frac{L^\#(B0) B1 A G0}{B a^6} + \frac{B B0 L(A) B1 \exp3}{a^6} - \frac{L^\#(D0) B1 A F0}{B a^6} \\
& - \frac{D0 L^\#(F0) B1 A}{B a^6} - \frac{L(B) D0 B1 G0}{\sqrt{B} a^6} + \frac{\sqrt{B} L(B) D0 B1 \exp3}{a^6} + \frac{D0 L(B) F0 D1}{\sqrt{B} a^6} \\
& - \frac{B0 L(A) B1 G0}{a^6} - \frac{D0 C0 F0 D1}{a^6} + \frac{B B1 \exp3 F0 D0}{a^6} - \frac{\frac{1}{2} I h C0 L(L^\#(B))}{B a^7} \\
& + \frac{\frac{1}{2} I h C0 L^\#(L(B))}{B a^7} + \frac{I B0^2 C0 F0 D1}{a^6} + \frac{I B0 D0 B1 G0}{a^6} - \frac{I B0 h B1 C0}{a^7} \\
& - \frac{I B0 D0 B1 A F0}{\sqrt{B} a^6} - \frac{\sqrt{B} B0 A C0 B1 \exp3}{a^6} - \frac{B0 A C0 F0 D1}{\sqrt{B} a^6} + \frac{\sqrt{B} D0 F0 G B0 C0}{a^6} \\
& + \frac{D0 F0 K B1 C0}{\sqrt{B} a^6} + \frac{D0 F0 K B1 A}{B a^6} + \frac{1}{2} \frac{L^\#(B) B1 A F0 D0}{B^2 a^6} + \frac{1}{2} \frac{L^\#(B) B1 A B0 G0}{B^2 a^6} \\
& + \frac{1}{2} \frac{L^\#(B) B1 C0 F0 D0}{B^{3/2} a^6} + \frac{1}{2} \frac{L^\#(B) B1 \exp3 B0 C0}{\sqrt{B} a^6} + \frac{1}{2} \frac{L^\#(B) D1 B0 C0 F0}{B^{3/2} a^6} \\
& + \frac{D0 F0 L(B) B0 C0}{\sqrt{B} a^6} - \frac{I B0 D0 B1 C0 F0}{a^6} - \frac{\frac{1}{2} I L(L^\#(B)) C0 F0 D0}{B a^6} \\
& + \frac{I B B0^2 C0 B1 \exp3}{a^6} - \frac{I B B0 D0 B1 \exp3}{a^6} + \frac{\frac{1}{2} I L^\#(L(B)) C0 F0 D0}{B a^6} \\
& + \frac{I B0^2 G0 B1 A}{\sqrt{B} a^6} - \frac{I B0 h B1 A}{\sqrt{B} a^7} + \frac{D0 G0 D1}{a^6} + \frac{D0 F0^2 D1}{a^6} + \frac{B B1 \exp3 h}{a^7} \\
& + \frac{D1 F0 h}{a^7} + \frac{h1 F0 D0}{a^7} + \frac{L(B) D0 h1}{\sqrt{B} a^7} + \frac{D0 A h1}{\sqrt{B} a^7} + \frac{B^{3/2} B0^2 E C0}{a^6} \\
& + \frac{\sqrt{B} B0 Lr G0}{a^6} - \frac{B^{3/2} B0 E D0}{a^6} - \frac{\sqrt{B} B0 H D1}{a^6} - \frac{\sqrt{B} D0 Pr C0}{a^6} + \frac{\sqrt{B} D0 F0 Tr}{a^6}
\end{aligned}$$

$$\begin{aligned}
& - \frac{\sqrt{B} F0 G D0^2}{a^6} + \frac{h Nr G0}{\sqrt{B} a^7} - \frac{\sqrt{B} h G D0}{a^7} - \frac{h K D1}{\sqrt{B} a^7} - \frac{D0 J D1}{a^6} + \frac{D0 Mr G0}{a^6} \\
& - \frac{B B0 OR C0}{a^6} + \frac{2 D0 F0 h}{a^7} - \frac{D0 C0 h1}{a^7} - \frac{D0 C0 h}{a^7} - \frac{h B0 G0}{a^7} - \frac{h B1 G0}{a^7} \\
& - \frac{h Qr C0}{a^7} - \frac{C0 F0 D0^2}{a^6} + \frac{B0 L(A) h1}{a^7} - \frac{1}{2} \frac{F0 L(B) D0^2}{\sqrt{B} a^6} - \frac{1}{2} \frac{D0 L(B) h}{\sqrt{B} a^7} \\
& - \frac{1}{2} \frac{L^\#(B) D1 h}{B^{3/2} a^7} + \frac{D0 L^\#(F0) D1}{\sqrt{B} a^6} - \frac{\sqrt{B} L^\#(D0) B1 exp3}{a^6} - \frac{\sqrt{B} L(B0) D0 G0}{a^6} \\
& - \frac{L^\#(B0) D1 G0}{\sqrt{B} a^6} + \frac{1}{2} \frac{S(B) B0 G0}{\sqrt{B} a^6} + \frac{1}{2} \frac{S(B) F0 D0}{\sqrt{B} a^6} + \frac{\sqrt{B} L(D0) B0 G0}{a^6} \\
& + \frac{L^\#(D0) B1 G0}{\sqrt{B} a^6} + \frac{\sqrt{B} C0 L(B0) h}{a^7} + \frac{C0 L^\#(B0) h1}{\sqrt{B} a^7} - \frac{1}{2} \frac{R(B) B0 C0}{a^6} \\
& - \frac{I L^\#(L(D0)) C0 F0}{a^6} - \frac{I B0^2 G0 D1}{a^6} - \frac{I B0 D0 h1}{a^7} + \frac{I B0 h D1}{a^7} + \frac{I B0^2 C0 h1}{a^7} \\
& + \frac{I L(L^\#(D0)) C0 F0}{a^6} + \frac{I D0 C0 L(L^\#(F0))}{a^6} - \frac{I D0 C0 L^\#(L(F0))}{a^6} + \frac{1}{2} \frac{S(B) h}{\sqrt{B} a^7} \\
& - \frac{\sqrt{B} D0 S(F0)}{a^6} - \frac{L^\#(D0) h1}{\sqrt{B} a^7} + \frac{\sqrt{B} L(F0) D0^2}{a^6} - \frac{\sqrt{B} L(D0) h}{a^7} \\
& - \frac{\sqrt{B} S(D0) F0}{a^6} + \frac{\sqrt{B} S(B0) G0}{a^6} + \frac{F0^2 D0^2}{a^6} - \frac{B F D0^2}{a^6} + \frac{G0 D0^2}{a^6} + \frac{B D0 Sr}{a^6} \\
& - \frac{B C0 R(B0)}{a^6} + \frac{B^{3/2} B0 Rr}{a^6} + \frac{\sqrt{B} h Tr}{a^7} + \frac{h1 h}{a^8} \Big) \tau \wedge \sigma + \left( - \frac{B^{3/2} B0^2 E}{a^5} + \frac{D0 h}{a^6} \right. \\
& + \frac{D0 h1}{a^6} + \frac{\sqrt{B} D0 Pr}{a^5} - \frac{L^\#(B0) h1}{a^6 \sqrt{B}} - \frac{\sqrt{B} L(B0) h}{a^6} - \frac{\sqrt{B} S(B0) F0}{a^5} + \frac{B B0 OR}{a^5} \\
& + \frac{h Qr}{a^6} + \frac{1}{2} \frac{B0 R(B)}{a^5} + \frac{I D0 L^\#(L(F0))}{a^5} - \frac{I D0 L(L^\#(F0))}{a^5} - \frac{I B0^2 h1}{a^6}
\end{aligned}$$

$$\begin{aligned}
& + \frac{BR(B0)}{a^5} - \frac{1}{2} \frac{D0F0L^\#(B)BI}{a^5B^{3/2}} + \frac{B0L(A)F0BI}{a^5} - \frac{L^\#(B0)BI A F0}{a^5B} \\
& + \frac{B0BI A^2F0}{a^5B} - \frac{1}{2} \frac{B0L^\#(B)BI \exp3}{a^5\sqrt{B}} + \frac{D0F0BI L(B)}{a^5\sqrt{B}} - \frac{\sqrt{B}D0F0GB0}{a^5} \\
& - \frac{D0F0KBI}{a^5\sqrt{B}} + \frac{2D0BI AF0}{a^5\sqrt{B}} - \frac{1}{2} \frac{D0F0L(B)B0}{a^5\sqrt{B}} + \frac{\sqrt{B}B0ABI \exp3}{a^5} \\
& + \frac{\frac{1}{2}ID0F0L(L^\#(B))}{a^5B} - \frac{\frac{1}{2}ID0F0L^\#(L(B))}{a^5B} - \frac{IBB0^2BI \exp3}{a^5} \\
& - \frac{1}{2} \frac{B0L^\#(B)BI A F0}{a^5B^2} - \frac{IBB0^2BI A F0}{a^5\sqrt{B}} - \frac{\sqrt{B}hGB0}{a^6} - \frac{hKBI}{a^6\sqrt{B}} + \frac{B0AhI}{a^6\sqrt{B}} \\
& + \frac{D0F0^2B0}{a^5} + \frac{D0F0^2BI}{a^5} + \frac{D0F0Qr}{a^5} + \frac{BD0BI \exp3}{a^5} - \frac{D0MrF0}{a^5} - \frac{BD0FB0}{a^5} \\
& - \frac{D0JBI}{a^5} - \frac{hL(B)B0}{a^6\sqrt{B}} - \frac{hNrF0}{a^6\sqrt{B}} - \frac{D0F0^2Nr}{a^5\sqrt{B}} + \frac{D0L^\#(F0)BI}{a^5\sqrt{B}} \\
& + \frac{\sqrt{B}D0L(F0)B0}{a^5} - \frac{\sqrt{B}B0HBI}{a^5} + \frac{hF0B0}{a^6} + \frac{hF0BI}{a^6} - \frac{\sqrt{B}L^\#(B0)BI \exp3}{a^5} \\
& - \frac{\sqrt{B}B0LrF0}{a^5} - \frac{1}{2} \frac{L^\#(B)BI h}{a^6B^{3/2}} - \frac{1}{2} \frac{B0L^\#(B)hI}{a^6B^{3/2}} - \frac{1}{2} \frac{B0S(B)F0}{a^5\sqrt{B}} \\
& + \frac{IBB0BI h}{a^6} - \frac{\frac{1}{2}IL^\#(L(B)) h}{a^6B} + \frac{\frac{1}{2}IL(L^\#(B)) h}{a^6B} \Big) \tau \wedge \rho + \left( \frac{\sqrt{B}F0GD0}{a^4} \right. \\
& - \frac{1}{2} \frac{L^\#(B)BI G0}{a^4B^{3/2}} + \frac{1}{2} \frac{L^\#(B)BI \exp3}{a^4\sqrt{B}} + \frac{C0F0D0}{a^4} + \frac{\sqrt{B}hG}{a^5} + \frac{\sqrt{B}L(B0)G0}{a^4} \\
& + \frac{IB0hI}{a^5} + \frac{1}{2} \frac{F0L(B)D0}{a^4\sqrt{B}} - \frac{\frac{1}{2}IL^\#(L(B))G0}{a^4B} + \frac{\frac{1}{2}IL(L^\#(B))G0}{a^4B} - \frac{1}{2} \frac{R(B)}{a^4} \\
& - \frac{F0^2D0}{a^4} + \frac{1}{2} \frac{L^\#(B)hI}{a^5B^{3/2}} + \frac{1}{2} \frac{S(B)F0}{a^4\sqrt{B}} - \frac{F0h}{a^5} + \frac{L(B)h}{a^5\sqrt{B}} - \frac{\sqrt{B}L(F0)D0}{a^4}
\end{aligned}$$

$$\begin{aligned}
& - \frac{G0D0}{a^4} + \frac{BFD0}{a^4} + \frac{1}{2} \frac{L^\#(B) B1 A F0}{a^4 B^2} + \frac{1}{2} \frac{L^\#(B) B1 C0 F0}{a^4 B^{3/2}} \\
& - \frac{\frac{1}{2} I F0 C0 L(L^\#(B))}{a^4 B} + \frac{\frac{1}{2} I F0 C0 L^\#(L(B))}{a^4 B} + \frac{B^{3/2} E B0}{a^4} + \frac{I B B0 B1 exp3}{a^4} \\
& + \left. \frac{I B0 B1 C0 F0}{a^4} + \frac{I B0 B1 A F0}{a^4 \sqrt{B}} - \frac{\sqrt{B} L(B) C0 F0}{a^4} - \frac{I B0 B1 G0}{a^4} \right) \tau \wedge \zeta \\
& + \left( \frac{1}{2} \frac{D0 L^\#(B) F0}{a^4 B^{3/2}} - \frac{F0^2 D0}{a^4} + \frac{D0 F0 K}{a^4 \sqrt{B}} - \frac{D0 L^\#(F0)}{a^4 \sqrt{B}} - \frac{G0 D0}{a^4} + \frac{C0 F0 D0}{a^4} \right. \\
& - \frac{F0 L(B) D0}{a^4 \sqrt{B}} - \frac{D0 A F0}{a^4 \sqrt{B}} + \frac{D0 J}{a^4} + \frac{I B0^2 G0}{a^4} - \frac{I B0 h}{a^5} - \frac{I B0^2 C0 F0}{a^4} - \frac{B0 A G0}{a^4 \sqrt{B}} \\
& + \frac{B0 A C0 F0}{a^4 \sqrt{B}} - \frac{B0 L(A) F0}{a^4} + \frac{\sqrt{B} B0 H}{a^4} + \frac{L^\#(B0) G0}{a^4 \sqrt{B}} - \frac{L^\#(B0) C0 F0}{a^4 \sqrt{B}} \\
& \left. + \frac{1}{2} \frac{L^\#(B) h}{a^5 B^{3/2}} + \frac{1}{2} \frac{L^\#(B) B0 G0}{a^4 B^{3/2}} - \frac{1}{2} \frac{L^\#(B) B0 C0 F0}{a^4 B^{3/2}} - \frac{F0 h}{a^5} + \frac{h K}{a^5 \sqrt{B}} \right) \tau \wedge \zeta^\# \\
& + \left( \frac{h N r}{a^5 \sqrt{B}} - \frac{h B1}{a^5} + \frac{D0 D1}{a^4} + \frac{\sqrt{B} B0 L r}{a^4} + \frac{D0 M r}{a^4} - \frac{L^\#(B0) D1}{a^4 \sqrt{B}} \right. \\
& + \frac{\sqrt{B} L(D0) B0}{a^4} - \frac{\sqrt{B} L(B0) D0}{a^4} + \frac{L^\#(D0) B1}{a^4 \sqrt{B}} + \frac{1}{2} \frac{B0 S(B)}{a^4 \sqrt{B}} - \frac{I B0^2 D1}{a^4} \\
& - \frac{B0 h}{a^5} + \frac{\sqrt{B} S(B0)}{a^4} + \frac{D0^2}{a^4} - \frac{I L(L^\#(D0))}{a^4} + \frac{I L^\#(L(D0))}{a^4} + \frac{1}{2} \frac{B0 L^\#(B) B1 A}{a^4 B^2} \\
& + \frac{I B0^2 B1 A}{a^4 \sqrt{B}} - \frac{B0 L(A) B1}{a^4} + \frac{D0 N r F0}{a^4 \sqrt{B}} + \frac{B0 A D1}{a^4 \sqrt{B}} + \frac{L^\#(B0) B1 A}{a^4 B} - \frac{B0 B1 A^2}{a^4 B} \\
& - \frac{D0 F0 B0}{a^4} - \frac{D0 F0 B1}{a^4} - \frac{1}{2} \frac{D0 L(B) B0}{a^4 \sqrt{B}} - \frac{1}{2} \frac{B0 L^\#(B) D1}{a^4 B^{3/2}} - \frac{B1 L(B) D0}{a^4 \sqrt{B}} \\
& \left. - \frac{2 B1 A D0}{a^4 \sqrt{B}} + \frac{I B0 B1 D0}{a^4} \right) \sigma \wedge \rho + \left( \frac{F0 D0}{a^3} + \frac{1}{2} \frac{L(B) D0}{a^3 \sqrt{B}} - \frac{C0 D0}{a^3} \right. \\
& - \frac{\sqrt{B} L(D0)}{a^3} + \frac{I B0 D1}{a^3} - \frac{I B0 B1 A}{a^3 \sqrt{B}} - \frac{I B0 B1 C0}{a^3} + \frac{\sqrt{B} L(B0) C0}{a^3} \\
& \left. + \frac{1}{2} \frac{L^\#(B) D1}{a^3 B^{3/2}} - \frac{1}{2} \frac{L^\#(B) B1 A}{a^3 B^2} - \frac{1}{2} \frac{L^\#(B) B1 C0}{a^3 B^{3/2}} + \frac{\frac{1}{2} I C0 L(L^\#(B))}{a^3 B} \right)
\end{aligned}$$

$$\begin{aligned}
& - \frac{\frac{1}{2} I C 0 L^\#(L(B))}{a^3 B} - \frac{1}{2} \frac{S(B)}{a^3 \sqrt{B}} + \frac{h}{a^4} \left) \sigma \wedge \zeta + \left( \frac{F 0 D 0}{a^3} - \frac{C 0 D 0}{a^3} + \frac{L(B) D 0}{a^3 \sqrt{B}} \right. \\
& + \frac{D 0 A}{a^3 \sqrt{B}} - \frac{L^\#(D 0)}{a^3 \sqrt{B}} - \frac{I B 0 D 0}{a^3} + \frac{I B 0^2 C 0}{a^3} - \frac{B 0 A C 0}{a^3 \sqrt{B}} + \frac{B 0 L(A)}{a^3} + \frac{L^\#(B 0) C 0}{a^3 \sqrt{B}} \\
& + \frac{1}{2} \frac{L^\#(B) B 0 C 0}{a^3 B^{3/2}} + \frac{h}{a^4} \left) \sigma \wedge \zeta^\# + \left( \frac{D 0}{a^2} + \frac{I B 0 B 1}{a^2} - \frac{\sqrt{B} L(B 0)}{a^2} + \frac{1}{2} \frac{L^\#(B) B 1}{a^2 B^{3/2}} \right. \\
& - \frac{\frac{1}{2} I L(L^\#(B))}{a^2 B} + \frac{\frac{1}{2} I L^\#(L(B))}{a^2 B} \left) \rho \wedge \zeta + \left( \frac{D 0}{a^2} - \frac{I B 0^2}{a^2} + \frac{B 0 A}{a^2 \sqrt{B}} - \frac{L^\#(B 0)}{a^2 \sqrt{B}} \right. \\
& \left. - \frac{1}{2} \frac{L^\#(B) B 0}{a^2 B^{3/2}} \right) \rho \wedge \zeta^\# + \left( \frac{I B 0}{a} + \frac{1}{2} \frac{L^\#(B)}{a B^{3/2}} \right) \zeta \wedge \zeta^\#
\end{aligned}$$

**frame2** > result(SE[5]);

$$\begin{aligned}
& \alpha_1 \wedge \zeta^\# + \alpha_3 \wedge \tau + \left( \frac{\sqrt{B} B 1 \exp 3 N r G 0}{a^6} - \frac{B^{3/2} B 1 \exp 3 G D 0}{a^6} - \frac{\sqrt{B} B 1 \exp 3 K D 1}{a^6} \right. \\
& + \frac{\sqrt{B} B 1^2 \exp 3 K C 0}{a^6} - \frac{B 1 A M r G 0}{\sqrt{B} a^6} + \frac{\sqrt{B} B 1 A F D 0}{a^6} + \frac{2 B 1 A J D 1}{\sqrt{B} a^6} \\
& - \frac{B 1^2 A J C 0}{\sqrt{B} a^6} + \frac{B^{3/2} B 1 E B 0 C 0}{a^6} + \frac{D 1 F 0 N r G 0}{\sqrt{B} a^6} - \frac{\sqrt{B} D 1 F 0 G D 0}{a^6} \\
& - \frac{2 D 1 G 0 B 1 A}{\sqrt{B} a^6} + \frac{\sqrt{B} D 1 A B 1 \exp 3}{a^6} + \frac{B 1 A C 0 h}{\sqrt{B} a^7} + \frac{\sqrt{B} h 1 G B 0 C 0}{a^7} \\
& + \frac{h 1 K B 1 C 0}{\sqrt{B} a^7} + \frac{1}{2} \frac{D 1 L^\#(B) B 1 \exp 3}{\sqrt{B} a^6} + \frac{B^{3/2} B 1 R r}{a^6} + \frac{D 1 F 0 K B 1 A}{B a^6} \\
& + \frac{D 1 L^\#(B) B 1 C 0 F 0}{B^{3/2} a^6} + \frac{1}{2} \frac{\sqrt{B} L(B) B 0 C 0 B 1 \exp 3}{a^6} + \frac{3}{2} \frac{L(B) B 0 C 0 F 0 D 1}{\sqrt{B} a^6} \\
& - \frac{1}{2} \frac{L(B) D 0 B 1 C 0 F 0}{\sqrt{B} a^6} - \frac{B 1 A L(B) F 0 D 1}{B a^6} + \frac{3}{2} \frac{B 1 A L(B) B 0 G 0}{B a^6} \\
& - \frac{3}{2} \frac{F 0 A B 1 L(B) D 0}{B a^6} + \frac{B 1 A C 0 F 0 D 0}{\sqrt{B} a^6} - \frac{\sqrt{B} B 1 A F B 0 C 0}{a^6}
\end{aligned} \tag{9}$$

$$\begin{aligned}
& + \frac{B^{3/2} B1 \exp3 G B0 C0}{a^6} + \frac{\sqrt{B} D1 F0 G B0 C0}{a^6} + \frac{D1 F0 K B1 C0}{\sqrt{B} a^6} \\
& + \frac{I B B0 C0 B1^2 \exp3}{a^6} + \frac{\frac{3}{2} I L^\#(L(B)) C0 F0 D1}{B a^6} - \frac{\frac{3}{2} I L(L^\#(B)) C0 F0 D1}{B a^6} \\
& + \frac{\frac{3}{2} I B1 A L^\#(L(B)) G0}{B^{3/2} a^6} - \frac{\frac{3}{2} I B1 A L(L^\#(B)) G0}{B^{3/2} a^6} - \frac{I D0 B1^2 A F0}{\sqrt{B} a^6} \\
& + \frac{I B0 G0 B1^2 A}{\sqrt{B} a^6} + \frac{I B1 B0 C0 F0 D1}{a^6} - \frac{A \exp3 L^\#(B) B1^2}{B a^6} - \frac{A L(B1) B0 G0}{a^6} \\
& + \frac{B1^2 \exp3 K A}{a^6} + \frac{2 B B1 \exp3 F0 D1}{a^6} - \frac{B B1 \exp3 B0 G0}{a^6} - \frac{B B1 \exp3 Qr C0}{a^6} \\
& + \frac{B1 A Pr C0}{a^6} - \frac{B1 A^2 F0 D1}{B a^6} - \frac{B D1 C0 B1 \exp3}{a^6} + \frac{B D1 F B0 C0}{a^6} + \frac{D1 J B1 C0}{a^6} \\
& - \frac{D1 F0 B0 G0}{a^6} - \frac{D1 F0 B1 G0}{a^6} - \frac{D1 F0 Qr C0}{a^6} + \frac{h1 K B1 A}{B a^7} - \frac{I h B1^2 A}{\sqrt{B} a^7} \\
& + \frac{I L(L^\#(B)) G0 D1}{B a^6} - \frac{I L^\#(L(B)) G0 D1}{B a^6} - \frac{I B D0 B1^2 \exp3}{a^6} \\
& + \frac{I B B1 L(L^\#(\exp3)) C0}{a^6} - \frac{I B \exp3 L^\#(L(B1)) C0}{a^6} + \frac{I B \exp3 L(L^\#(B1)) C0}{a^6} \\
& - \frac{I B B1 L^\#(L(\exp3)) C0}{a^6} + \frac{\frac{3}{2} I C0 L^\#(L(B)) h1}{B a^7} - \frac{\frac{3}{2} I C0 L(L^\#(B)) h1}{B a^7} \\
& - \frac{I A L^\#(L(B1)) G0}{\sqrt{B} a^6} + \frac{I A L(L^\#(B1)) G0}{\sqrt{B} a^6} + \frac{I B1 L(L^\#(A)) G0}{\sqrt{B} a^6} - \frac{I B1 L^\#(L(A)) G0}{\sqrt{B} a^6} \\
& + \frac{\frac{1}{2} I C0 L^\#(L(B)) B1 \exp3}{a^6} + \frac{I B1 B0 C0 h1}{a^7} - \frac{I D0 B1^2 C0 F0}{a^6} - \frac{I B1 B0 G0 D1}{a^6} \\
& - \frac{\frac{1}{2} I C0 L(L^\#(B)) B1 \exp3}{a^6} - \frac{B^{3/2} \exp3 L(B1) B0 C0}{a^6} + \frac{h1 L^\#(B) B1 C0}{B^{3/2} a^7}
\end{aligned}$$



$$\begin{aligned}
& + \frac{AL^\#(B)BI^2G0}{B^2a^6} - \frac{BIAL(B)hl}{Ba^7} - \frac{3}{2} \frac{BIAL(B)h}{Ba^7} - \frac{BI^2AL(B)exp3}{a^6} \\
& - \frac{D1L^\#(F0)BIA}{Ba^6} + \frac{F0BIL^\#(A)D1}{Ba^6} + \frac{F0AL^\#(B1)D1}{Ba^6} + \frac{F0AL(B1)D0}{a^6} \\
& + \frac{F0BIL(A)D0}{a^6} + \frac{BIL(A)F0D1}{a^6} + \frac{BI^2AL(B)G0}{Ba^6} - \frac{L^\#(D1)BIAF0}{Ba^6} \\
& - \frac{\sqrt{B}D1PrC0}{a^6} + \frac{\sqrt{B}D1F0Tr}{a^6} - \frac{F0KDI^2}{\sqrt{B}a^6} + \frac{AF0DI^2}{\sqrt{B}a^6} + \frac{B^{3/2}BIexp3Tr}{a^6} \\
& + \frac{DIAhl}{\sqrt{B}a^7} - \frac{\sqrt{B}BIA Sr}{a^6} + \frac{\sqrt{B}HBI^2C0}{a^6} + \frac{\sqrt{B}BILrG0}{a^6} - \frac{B^{3/2}BIED0}{a^6} \\
& - \frac{\sqrt{B}BIHDI}{a^6} + \frac{hlNrG0}{\sqrt{B}a^7} - \frac{\sqrt{B}hlGD0}{a^7} - \frac{hlKDI}{\sqrt{B}a^7} - \frac{BBIORC0}{a^6} \\
& + \frac{G0BI^2A^2}{Ba^6} + \frac{HBI^2A}{a^6} - \frac{BBI^2exp3G0}{a^6} - \frac{BI^2A^2J}{Ba^6} - \frac{BI^2A^2exp3}{a^6} - \frac{C0F0DI^2}{a^6} \\
& + \frac{D1MrG0}{a^6} - \frac{BD1FD0}{a^6} + \frac{2BBIexp3hl}{a^7} - \frac{BI^2hl}{Ba^7} - \frac{D1C0h}{a^7} - \frac{D1C0hl}{a^7} \\
& + \frac{2D1F0hl}{a^7} - \frac{hlB0G0}{a^7} - \frac{hlB1G0}{a^7} - \frac{hlQrC0}{a^7} + \frac{1}{2} \frac{R(B)B1C0}{a^6} \\
& - \frac{L(A)BI^2G0}{a^6} + \frac{BL(A)BI^2exp3}{a^6} - \frac{AL^\#(exp3)BI^2}{a^6} + \frac{exp3L^\#(A)BI^2}{a^6} \\
& - \frac{L^\#(A)BI^2G0}{Ba^6} + \frac{BIL(A)h}{a^7} + \frac{BIL^\#(A)hl}{Ba^7} + \frac{BIL(A)hl}{a^7} + \frac{AL^\#(B1)hl}{Ba^7} \\
& + \frac{AL(B1)h}{a^7} + \frac{D1L(B)hl}{\sqrt{B}a^7} + \frac{1}{2} \frac{\sqrt{B}S(B)BIexp3}{a^6} - \frac{\sqrt{B}C0L^\#(exp3)BI^2}{a^6} \\
& + \frac{\sqrt{B}BIL^\#(exp3)D1}{a^6} + \frac{B^{3/2}BIL(exp3)D0}{a^6} + \frac{\sqrt{B}exp3L^\#(B1)D1}{a^6}
\end{aligned}$$

$$\begin{aligned}
& + \frac{B^{3/2} \exp 3 L(B1) D0}{a^6} - \frac{1}{2} \frac{D1 L^\#(B) h1}{B^{3/2} a^7} + \frac{L^\#(D1) B1 G0}{\sqrt{B} a^6} - \frac{\sqrt{B} L^\#(D1) B1 \exp 3}{a^6} \\
& + \frac{\sqrt{B} L(D1) B0 G0}{a^6} - \frac{L^\#(B1) D1 G0}{\sqrt{B} a^6} - \frac{\sqrt{B} L(B1) D0 G0}{a^6} + \frac{3}{2} \frac{S(B) F0 D1}{\sqrt{B} a^6} \\
& - \frac{1}{2} \frac{S(B) B1 G0}{\sqrt{B} a^6} + \frac{3}{2} \frac{B1 A R(B)}{\sqrt{B} a^6} - \frac{1}{2} \frac{D1 L^\#(B) B1 G0}{B^{3/2} a^6} - \frac{B^{3/2} B1 L(\exp 3) B0 C0}{a^6} \\
& - \frac{D1 L(B) B1 G0}{\sqrt{B} a^6} + \frac{\sqrt{B} D1 L(B) B1 \exp 3}{a^6} - \frac{1}{2} \frac{L(B) h B1 C0}{\sqrt{B} a^7} - \frac{D1 L^\#(F0) B1 C0}{\sqrt{B} a^6} \\
& - \frac{\sqrt{B} D1 L(F0) B0 C0}{a^6} + \frac{L^\#(B1) D1 C0 F0}{\sqrt{B} a^6} + \frac{\sqrt{B} L(B1) D0 C0 F0}{a^6} \\
& - \frac{L(B) B0 G0 D1}{\sqrt{B} a^6} - \frac{L^\#(D1) B1 C0 F0}{\sqrt{B} a^6} - \frac{\sqrt{B} L(D1) B0 C0 F0}{a^6} + \frac{3}{2} \frac{L(B) B0 C0 h1}{\sqrt{B} a^7} \\
& + \frac{h1^2}{a^8} + \frac{B R(D1)}{a^6} + \frac{\sqrt{B} h1 Tr}{a^7} + \frac{B^2 B1^2 \exp 3^2}{a^6} + \frac{B D1 Sr}{a^6} + \frac{G0 D1^2}{a^6} - \frac{J D1^2}{a^6} \\
& + \frac{F0^2 D1^2}{a^6} - \frac{B C0 R(B1)}{a^6} - \frac{R(B) D1}{a^6} - \frac{\sqrt{B} L(D1) h}{a^7} + \frac{\sqrt{B} S(B1) G0}{a^6} \\
& - \frac{\sqrt{B} A R(B1)}{a^6} - \frac{\sqrt{B} B1 R(A)}{a^6} - \frac{\sqrt{B} D1 S(F0)}{a^6} + \frac{L^\#(F0) D1^2}{\sqrt{B} a^6} - \frac{\sqrt{B} S(D1) F0}{a^6} \\
& - \frac{B^{3/2} B1 S(\exp 3)}{a^6} - \frac{B^{3/2} \exp 3 S(B1)}{a^6} + \frac{3}{2} \frac{S(B) h1}{\sqrt{B} a^7} - \frac{L^\#(D1) h1}{\sqrt{B} a^7} \\
& - \frac{1 L(L^\#(D1)) G0}{a^6} + \frac{1 L^\#(L(D1)) G0}{a^6} - \frac{1}{2} \frac{F0 L^\#(B) D1^2}{B^{3/2} a^6} + \frac{L(B) F0 D1^2}{\sqrt{B} a^6} \\
& + \frac{\sqrt{B} D1 L(F0) D0}{a^6} + \frac{C0 L^\#(B1) h1}{\sqrt{B} a^7} + \frac{\sqrt{B} C0 L(B1) h}{a^7} + \frac{L(B) h D1}{\sqrt{B} a^7} \\
& + \frac{1 L(L^\#(D1)) C0 F0}{a^6} - \frac{1 L^\#(L(D1)) C0 F0}{a^6} + \frac{1 D0 B1^2 G0}{a^6} - \frac{1 B1 D0 h1}{a^7}
\end{aligned}$$

$$\begin{aligned}
& + \frac{IB1 h DI}{a^7} - \frac{Ih BI^2 C0}{a^7} + \frac{ID1 C0 L(L^\#(F0))}{a^6} - \frac{ID1 C0 L^\#(L(F0))}{a^6} \\
& - \frac{B1 A G0 D0}{\sqrt{B} a^6} + \frac{1}{2} \frac{L(B) D0 B1 G0}{\sqrt{B} a^6} - \frac{1}{2} \frac{\sqrt{B} L(B) D0 B1 exp3}{a^6} \\
& - \frac{1}{2} \frac{D0 L(B) F0 D1}{\sqrt{B} a^6} - \frac{B0 L(A) B1 G0}{a^6} - \frac{D0 C0 F0 D1}{a^6} + \frac{B B1 exp3 F0 D0}{a^6} \\
& + \frac{D0 G0 D1}{a^6} + \frac{D0 F0^2 D1}{a^6} + \frac{B B1 exp3 h}{a^7} + \frac{D1 F0 h}{a^7} + \frac{h1 F0 D0}{a^7} \\
& - \frac{3}{2} \frac{L(B) D0 h1}{\sqrt{B} a^7} + \frac{h1 h}{a^8} \left) \tau \wedge \sigma + \left( \frac{\sqrt{B} D1 Pr}{a^5} + \frac{\sqrt{B} L^\#(exp3) B1^2}{a^5} \right. \\
& - \frac{\sqrt{B} L(B1) h}{a^6} - \frac{L^\#(B1) h1}{a^6 \sqrt{B}} + \frac{B B1 OR}{a^5} - \frac{1}{2} \frac{R(B) B1}{a^5} - \frac{\sqrt{B} S(B1) F0}{a^5} \\
& - \frac{\sqrt{B} H B1^2}{a^5} + \frac{D1 h}{a^6} + \frac{D1 h1}{a^6} + \frac{h1 Qr}{a^6} + \frac{I B1^2 h}{a^6} + \frac{I D1 L^\#(L(F0))}{a^5} \\
& - \frac{I D1 L(L^\#(F0))}{a^5} - \frac{3}{2} \frac{F0 B1 A L(B) B0}{a^5 B} + \frac{\frac{3}{2} I B1 A F0 L(L^\#(B))}{a^5 B^{3/2}} \\
& - \frac{\frac{3}{2} I B1 A F0 L^\#(L(B))}{a^5 B^{3/2}} - \frac{I B0 B1^2 A F0}{a^5 \sqrt{B}} - \frac{F0 A L^\#(B) B1^2}{a^5 B^2} - \frac{B1^2 A F0 L(B)}{a^5 B} \\
& + \frac{B B1 exp3 F0 B0}{a^5} - \frac{1}{2} \frac{\sqrt{B} L(B) B0 B1 exp3}{a^5} + \frac{F0 A L(B1) B0}{a^5} \\
& - \frac{\sqrt{B} B1 exp3 Nr F0}{a^5} - \frac{B^{3/2} B1 exp3 G B0}{a^5} + \frac{D1 F0 B1 L(B)}{a^5 \sqrt{B}} - \frac{\sqrt{B} D1 F0 G B0}{a^5} \\
& - \frac{D1 F0 K B1}{a^5 \sqrt{B}} + \frac{2 D1 B1 A F0}{a^5 \sqrt{B}} - \frac{1}{2} \frac{D1 F0 L(B) B0}{a^5 \sqrt{B}} - \frac{1}{2} \frac{D1 F0 L^\#(B) B1}{a^5 B^{3/2}} \\
& + \frac{B1 A Mr F0}{a^5 \sqrt{B}} + \frac{\sqrt{B} B1 A F B0}{a^5} - \frac{I B B0 B1^2 exp3}{a^5} - \frac{I F0 B1 L(L^\#(A))}{a^5 \sqrt{B}}
\end{aligned}$$

$$\begin{aligned}
& + \frac{IF0AL^\#(L(B1))}{a^5\sqrt{B}} - \frac{IF0AL(L^\#(B1))}{a^5\sqrt{B}} + \frac{IF0B1L^\#(L(A))}{a^5\sqrt{B}} \\
& - \frac{\frac{1}{2}IDI F0L^\#(L(B))}{a^5B} + \frac{\frac{1}{2}IDI F0L(L^\#(B))}{a^5B} + \frac{BR(B1)}{a^5} - \frac{\sqrt{B}B1LrF0}{a^5} \\
& + \frac{D1F0^2B0}{a^5} + \frac{D1F0^2B1}{a^5} + \frac{D1F0Qr}{a^5} + \frac{BD1B1exp3}{a^5} - \frac{D1MrF0}{a^5} - \frac{BD1FB0}{a^5} \\
& - \frac{D1JB1}{a^5} + \frac{1}{2} \frac{B1S(B)F0}{a^5\sqrt{B}} - \frac{B^{3/2}B1EB0}{a^5} - \frac{\sqrt{B}B1^2exp3K}{a^5} + \frac{F0L^\#(A)B1^2}{a^5B} \\
& + \frac{L(A)F0B1^2}{a^5} - \frac{B1^2A^2F0}{a^5B} + \frac{1}{2} \frac{B1L(B)h}{a^6\sqrt{B}} - \frac{3}{2} \frac{L(B)B0h1}{a^6\sqrt{B}} + \frac{B1^2AJ}{a^5\sqrt{B}} \\
& - \frac{D1F0^2Nr}{a^5\sqrt{B}} + \frac{D1L^\#(F0)B1}{a^5\sqrt{B}} + \frac{\sqrt{B}D1L(F0)B0}{a^5} - \frac{B1Ah}{a^6\sqrt{B}} - \frac{B1APr}{a^5} \\
& + \frac{BB1exp3Qr}{a^5} - \frac{h1L^\#(B)B1}{a^6B^{3/2}} + \frac{h1F0B0}{a^6} + \frac{h1F0B1}{a^6} + \frac{BB1^2exp3F0}{a^5} \\
& + \frac{B^{3/2}B1L(exp3)B0}{a^5} + \frac{B^{3/2}exp3L(B1)B0}{a^5} - \frac{h1NrF0}{a^6\sqrt{B}} - \frac{\sqrt{B}h1GB0}{a^6} \\
& - \frac{h1KB1}{a^6\sqrt{B}} - \frac{\frac{1}{2}IL^\#(L(B))B1exp3}{a^5} - \frac{IB1B0h1}{a^6} + \frac{\frac{1}{2}IL(L^\#(B))B1exp3}{a^5} \\
& + \frac{IBB1L^\#(L(exp3))}{a^5} - \frac{IBB1L(L^\#(exp3))}{a^5} + \frac{IBexp3L^\#(L(B1))}{a^5} \\
& - \frac{IBexp3L(L^\#(B1))}{a^5} - \frac{\frac{3}{2}IL^\#(L(B))h1}{a^6B} + \frac{\frac{3}{2}IL(L^\#(B))h1}{a^6B} + \frac{B0L(A)F0B1}{a^5} \Big) \\
\tau \wedge \rho & + \left( \frac{C0F0D1}{a^4} - \frac{BF0B1exp3}{a^4} + \frac{G0B1A}{a^4\sqrt{B}} + \frac{BD1F}{a^4} - \frac{\sqrt{B}D1L(F0)}{a^4} \right. \\
& + \frac{B^{3/2}B1E}{a^4} + \frac{\sqrt{B}L(B1)G0}{a^4} - \frac{B^{3/2}B1L(exp3)}{a^4} - \frac{B^{3/2}exp3L(B1)}{a^4} + \frac{\sqrt{B}h1G}{a^5} \\
& \left. + \frac{IB1h1}{a^5} - \frac{IB1^2G0}{a^4} - \frac{1}{2} \frac{L(B)B1G0}{a^4\sqrt{B}} + \frac{1}{2} \frac{\sqrt{B}L(B)B1exp3}{a^4} + \frac{1}{2} \frac{L(B)F0D1}{a^4\sqrt{B}} \right)
\end{aligned}$$

$$\begin{aligned}
& + \frac{3}{2} \frac{L(B) B1 A F0}{a^4 B} + \frac{1 B1^2 A F0}{a^4 \sqrt{B}} - \frac{F0^2 D1}{a^4} - \frac{F0 h1}{a^5} + \frac{3}{2} \frac{L(B) h1}{a^5 \sqrt{B}} + \frac{1 B1^2 C0 F0}{a^4} \\
& + \frac{1 B B1^2 \exp3}{a^4} - \frac{G0 D1}{a^4} - \frac{C0 B1 A F0}{a^4 \sqrt{B}} + \frac{1}{2} \frac{C0 F0 B1 L(B)}{a^4 \sqrt{B}} - \frac{L(A) F0 B1}{a^4} \\
& + \frac{\sqrt{B} D1 F0 G}{a^4} - \frac{F0 A L(B1)}{a^4} - \frac{\sqrt{B} L(B1) C0 F0}{a^4} - \frac{\sqrt{B} B1 A F}{a^4} \\
& + \frac{B^{3/2} B1 \exp3 G}{a^4} \left) \tau \wedge \zeta + \left( \frac{F0 K D1}{a^4 \sqrt{B}} + \frac{C0 F0 D1}{a^4} - \frac{B F0 B1 \exp3}{a^4} - \frac{A F0 D1}{a^4 \sqrt{B}} \right. \\
& - \frac{\sqrt{B} B1 L^\#(\exp3)}{a^4} - \frac{\sqrt{B} \exp3 L^\#(B1)}{a^4} + \frac{h1 K}{a^5 \sqrt{B}} + \frac{L^\#(B1) G0}{a^4 \sqrt{B}} - \frac{1 B1 h}{a^5} \\
& + \frac{1}{2} \frac{F0 L^\#(B) D1}{a^4 B^{3/2}} + \frac{1}{2} \frac{L(B) B0 G0}{a^4 \sqrt{B}} - \frac{L(B) F0 D1}{a^4 \sqrt{B}} + \frac{L(B) B1 A F0}{a^4 B} \\
& - \frac{\frac{1}{2} I C0 F0 L^\#(L(B))}{a^4 B} + \frac{\frac{1}{2} I L(L^\#(B)) C0 F0}{a^4 B} - \frac{1 B1 B0 C0 F0}{a^4} - \frac{J B1 A}{a^4 \sqrt{B}} \\
& + \frac{1}{2} \frac{R(B)}{a^4} + \frac{J D1}{a^4} - \frac{F0^2 D1}{a^4} + \frac{L^\#(B) h1}{a^5 B^{3/2}} - \frac{1}{2} \frac{S(B) F0}{a^4 \sqrt{B}} - \frac{F0 h1}{a^5} - \frac{1}{2} \frac{L(B) h}{a^5 \sqrt{B}} \\
& - \frac{F0 B1 L^\#(A)}{a^4 B} - \frac{F0 A L^\#(B1)}{a^4 B} - \frac{L^\#(B1) C0 F0}{a^4 \sqrt{B}} + \frac{\sqrt{B} B1 \exp3 K}{a^4} + \frac{1 B1 B0 G0}{a^4} \\
& - \frac{\frac{1}{2} I L(L^\#(B)) G0}{a^4 B} + \frac{\frac{1}{2} I L^\#(L(B)) G0}{a^4 B} - \frac{L^\#(F0) D1}{a^4 \sqrt{B}} - \frac{G0 D1}{a^4} \\
& - \frac{1}{2} \frac{F0 L(B) B0 C0}{a^4 \sqrt{B}} + \frac{L^\#(B) B1 A F0}{a^4 B^2} + \frac{\sqrt{B} H B1}{a^4} + \frac{B1 A^2 F0}{a^4 B} - \frac{L(A) F0 B1}{a^4} \left. \right) \\
& \tau \wedge \zeta^\# + \left( \frac{D0 D1}{a^4} - \frac{B B1^2 \exp3}{a^4} + \frac{h1 N r}{a^5 \sqrt{B}} + \frac{\sqrt{B} B1 L r}{a^4} - \frac{L^\#(B1) D1}{a^4 \sqrt{B}} \right. \\
& - \frac{\sqrt{B} L(B1) D0}{a^4} - \frac{1}{2} \frac{B1 S(B)}{a^4 \sqrt{B}} + \frac{L^\#(D1) B1}{a^4 \sqrt{B}} + \frac{\sqrt{B} L(D1) B0}{a^4} + \frac{D1 M r}{a^4} \\
& + \frac{B1^2 A^2}{a^4 B} - \frac{L(A) B1^2}{a^4} - \frac{L^\#(A) B1^2}{a^4 B} - \frac{h1 B0}{a^5} + \frac{1 B1^2 D0}{a^4} + \frac{3}{2} \frac{B1 A L(B) B0}{a^4 B}
\end{aligned}$$

$$\begin{aligned}
& + \frac{\frac{3}{2} \text{IBI} A L^\#(L(B))}{a^4 B^{3/2}} - \frac{\frac{3}{2} \text{IBI} A L(L^\#(B))}{a^4 B^{3/2}} + \frac{\text{IB}0 \text{BI}^2 A}{a^4 \sqrt{B}} - \frac{\text{D}1 \text{F}0 \text{BI}}{a^4} \\
& - \frac{A L(B) \text{B}0}{a^4} + \frac{\text{BI}^2 A L(B)}{a^4 B} - \frac{B \text{BI} \text{exp}3 \text{B}0}{a^4} - \frac{\text{D}1 \text{F}0 \text{B}0}{a^4} - \frac{L(B) \text{B}0 \text{D}1}{a^4 \sqrt{B}} \\
& - \frac{\text{D}1 \text{BI} L(B)}{a^4 \sqrt{B}} - \frac{1}{2} \frac{\text{D}1 L^\#(B) \text{BI}}{a^4 B^{3/2}} + \frac{A L^\#(B) \text{BI}^2}{a^4 B^2} - \frac{\text{BI} A \text{M}r}{a^4 \sqrt{B}} + \frac{\sqrt{B} \text{BI} \text{exp}3 \text{N}r}{a^4} \\
& + \frac{\text{D}1 \text{N}r \text{F}0}{a^4 \sqrt{B}} - \frac{2 \text{D}1 \text{BI} A}{a^4 \sqrt{B}} - \frac{\text{IBI} \text{B}0 \text{D}1}{a^4} + \frac{\text{IBI} L(L^\#(A))}{a^4 \sqrt{B}} + \frac{\text{I} A L(L^\#(BI))}{a^4 \sqrt{B}} \\
& - \frac{\text{IBI} L^\#(L(A))}{a^4 \sqrt{B}} - \frac{\text{I} A L^\#(L(BI))}{a^4 \sqrt{B}} - \frac{\text{I} L^\#(L(B)) \text{D}1}{a^4 B} + \frac{\text{I} L(L^\#(B)) \text{D}1}{a^4 B} - \frac{\text{BI} h1}{a^5} \\
& + \frac{\sqrt{B} S(BI)}{a^4} + \frac{\text{D}1^2}{a^4} - \frac{\text{I} L(L^\#(D1))}{a^4} + \frac{\text{I} L^\#(L(D1))}{a^4} - \frac{\text{B}0 L(A) \text{BI}}{a^4} \\
& + \frac{1}{2} \left( \frac{\text{BI} L(B) \text{D}0}{a^4 \sqrt{B}} - \frac{\text{BI} A \text{D}0}{a^4 \sqrt{B}} \right) \sigma \wedge \rho + \left( \frac{\text{D}1 \text{F}0}{a^3} + \frac{L(B) \text{D}1}{a^3 \sqrt{B}} - \frac{\text{C}0 \text{D}1}{a^3} \right. \\
& - \frac{\sqrt{B} L(D1)}{a^3} + \frac{B \text{BI} \text{exp}3}{a^3} - \frac{3}{2} \frac{L(B) \text{BI} A}{a^3 B} + \frac{\text{C}0 \text{BI} A}{a^3 \sqrt{B}} + \frac{L(A) \text{BI}}{a^3} + \frac{A L(BI)}{a^3} \\
& \left. + \frac{\text{IBI} \text{D}1}{a^3} - \frac{\text{IBI}^2 A}{a^3 \sqrt{B}} - \frac{\text{IBI}^2 \text{C}0}{a^3} + \frac{\sqrt{B} L(BI) \text{C}0}{a^3} - \frac{1}{2} \frac{\text{C}0 \text{BI} L(B)}{a^3 \sqrt{B}} + \frac{h1}{a^4} \right) \sigma \wedge \zeta \\
& + \left( \frac{\text{D}1 \text{F}0}{a^3} + \frac{1}{2} \frac{L^\#(B) \text{D}1}{a^3 B^{3/2}} - \frac{\text{C}0 \text{D}1}{a^3} + \frac{L(B) \text{D}1}{a^3 \sqrt{B}} + \frac{A \text{D}1}{a^3 \sqrt{B}} - \frac{L^\#(D1)}{a^3 \sqrt{B}} \right. \\
& + \frac{B \text{BI} \text{exp}3}{a^3} - \frac{L^\#(B) \text{BI} A}{a^3 B^2} - \frac{L(B) \text{BI} A}{a^3 B} - \frac{\text{BI} A^2}{a^3 B} + \frac{\text{BI} L^\#(A)}{a^3 B} + \frac{A L^\#(BI)}{a^3 B} \\
& - \frac{\text{IBI} \text{D}0}{a^3} + \frac{1}{2} \frac{\text{I} \text{C}0 L^\#(L(B))}{a^3 B} + \frac{L(A) \text{BI}}{a^3} + \frac{L^\#(BI) \text{C}0}{a^3 \sqrt{B}} - \frac{1}{2} \frac{L(B) \text{D}0}{a^3 \sqrt{B}} \\
& \left. + \frac{1}{2} \frac{L(B) \text{B}0 \text{C}0}{a^3 \sqrt{B}} - \frac{1}{2} \frac{\text{I} \text{C}0 L(L^\#(B))}{a^3 B} + \frac{\text{IBI} \text{B}0 \text{C}0}{a^3} + \frac{1}{2} \frac{S(B)}{a^3 \sqrt{B}} + \frac{h1}{a^4} \right) \sigma \wedge \zeta^\# \\
& + \left( \frac{\text{D}1}{a^2} - \frac{\text{BI} A}{a^2 \sqrt{B}} + \frac{\text{IBI}^2}{a^2} - \frac{\sqrt{B} L(BI)}{a^2} + \frac{1}{2} \frac{\text{BI} L(B)}{a^2 \sqrt{B}} \right) \rho \wedge \zeta + \left( \frac{\text{D}1}{a^2} \right.
\end{aligned}$$

$$\begin{aligned}
& - \frac{1 B 0 B 1}{a^2} - \frac{L^\#(B 1)}{a^2 \sqrt{B}} - \frac{1}{2} \frac{L(B) B 0}{a^2 \sqrt{B}} + \frac{\frac{1}{2} 1 L(L^\#(B))}{a^2 B} - \frac{\frac{1}{2} 1 L^\#(L(B))}{a^2 B} \Big) \rho \wedge \zeta^\# \\
& + \left( \frac{1 B 1}{a} + \frac{1}{2} \frac{L(B)}{a \sqrt{B}} \right) \zeta \wedge \zeta^\#
\end{aligned}$$

**frame2** > *Torsion*(SE[4], 5, 8);

$$\begin{aligned}
& \frac{F 0 D 0}{a^3} - \frac{C 0 D 0}{a^3} + \frac{L(B) D 0}{a^3 \sqrt{B}} + \frac{D 0 A}{a^3 \sqrt{B}} - \frac{L^\#(D 0)}{a^3 \sqrt{B}} - \frac{1 B 0 D 0}{a^3} + \frac{1 B 0^2 C 0}{a^3} - \frac{B 0 A C 0}{a^3 \sqrt{B}} \\
& + \frac{B 0 L(A)}{a^3} + \frac{L^\#(B 0) C 0}{a^3 \sqrt{B}} + \frac{1}{2} \frac{L^\#(B) B 0 C 0}{a^3 B^{3/2}} + \frac{h}{a^4}
\end{aligned} \tag{10}$$

**frame2** > *Torsion*(SE[5], 5, 7);

$$\begin{aligned}
& \frac{D 1 F 0}{a^3} + \frac{L(B) D 1}{a^3 \sqrt{B}} - \frac{C 0 D 1}{a^3} - \frac{\sqrt{B} L(D 1)}{a^3} + \frac{B B 1 \exp 3}{a^3} - \frac{3}{2} \frac{L(B) B 1 A}{a^3 B} + \frac{C 0 B 1 A}{a^3 \sqrt{B}} \\
& + \frac{L(A) B 1}{a^3} + \frac{A L(B 1)}{a^3} + \frac{1 B 1 D 1}{a^3} - \frac{1 B 1^2 A}{a^3 \sqrt{B}} - \frac{1 B 1^2 C 0}{a^3} + \frac{\sqrt{B} L(B 1) C 0}{a^3} \\
& - \frac{1}{2} \frac{C 0 B 1 L(B)}{a^3 \sqrt{B}} + \frac{h 1}{a^4}
\end{aligned} \tag{11}$$

**frame2** > *expand*(*solve*(*Torsion*(SE[4], 5, 8), *h*));

$$\begin{aligned}
& -a D 0 F 0 + a C 0 D 0 - \frac{a D 0 L(B)}{\sqrt{B}} - \frac{a D 0 A}{\sqrt{B}} + \frac{a L^\#(D 0)}{\sqrt{B}} + 1 a B 0 D 0 - 1 a B 0^2 C 0 \\
& + \frac{a B 0 A C 0}{\sqrt{B}} - a B 0 L(A) - \frac{a L^\#(B 0) C 0}{\sqrt{B}} - \frac{1}{2} \frac{a L^\#(B) B 0 C 0}{B^{3/2}}
\end{aligned} \tag{12}$$

> *expand*(*solve*(*Torsion*(SE[5], 5, 7), *h 1*));

$$\begin{aligned}
& -a D 1 F 0 - \frac{a L(B) D 1}{\sqrt{B}} + a C 0 D 1 + a \sqrt{B} L(D 1) - a B B 1 \exp 3 + \frac{3}{2} \frac{a L(B) B 1 A}{B} \\
& - \frac{a C 0 B 1 A}{\sqrt{B}} - a L(A) B 1 - a A L(B 1) - 1 a B 1 D 1 + \frac{1 a B 1^2 A}{\sqrt{B}} + 1 a B 1^2 C 0 \\
& - a \sqrt{B} L(B 1) C 0 + \frac{1}{2} \frac{a C 0 B 1 L(B)}{\sqrt{B}}
\end{aligned} \tag{13}$$

**frame2** >